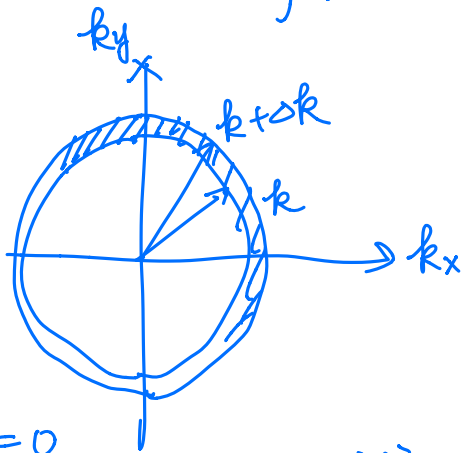


$$\alpha(\hbar\omega) = C_0 \frac{2}{V} \sum_{\mathbf{k}} \underbrace{\delta(E_e - E_h - \hbar\omega) \cdot |\mathbf{e} \cdot \mathbf{p}|^2 (f_v - f_c)}_{\text{transition probability}}$$

$$\rightarrow \int P_{r,20}(\hbar\omega) \cdot \delta(\hbar\omega - (E_e - E_h)) d\omega$$



$$E_v = 0$$

$$E_e = E_g + E_{el} + \frac{\hbar^2 k^2}{2m_e^*}$$

$$\rightarrow E_h = E_{v1} - \frac{\hbar^2 k^2}{2m_h^*}$$

$$E_e - E_h = \hbar\omega = \underbrace{E_g + E_{el} - E_{v1}}_{E_{g,eff}} + \frac{\hbar^2 k^2}{2} \left(\frac{1}{m_e^*} + \frac{1}{m_h^*} \right) = \frac{\hbar^2 k^2}{2m_r^*}$$

$$\hbar\omega = E_{g,eff} + \frac{\hbar^2 k^2}{2m_r^*}$$

$$\text{Kinetic Energy } E_k = \frac{\hbar^2 k^2}{2m_r^*}$$

↑ kinetic energy of the electron-hole pair connected by the photon

$$dE_k = \frac{2\hbar^2 k}{2m_r^*} \Delta k$$

Total 2-D k-space area for states with electron-hole kinetic energy = $\frac{\hbar^2 k^2}{2m_r^*}$

$$\frac{2}{V} \sum_{\mathbf{k}} = \frac{2}{L_x L_y L_z} \int \frac{2\pi k dk}{\left(\frac{2\pi}{L_x}\right) \left(\frac{2\pi}{L_y}\right)} = \frac{1}{L_z} \int \frac{4\pi k dk}{4\pi^2}$$

← area per state

$$= \frac{1}{L_z \pi} \int k dk = \frac{1}{L_z \pi} \cdot \frac{m_r^*}{\hbar^2} \int dE = \frac{m_r^*}{\pi \hbar^2 L_z} \int dE$$

In comparison, the electron 2D density of states is related only to electron kinetic energy:

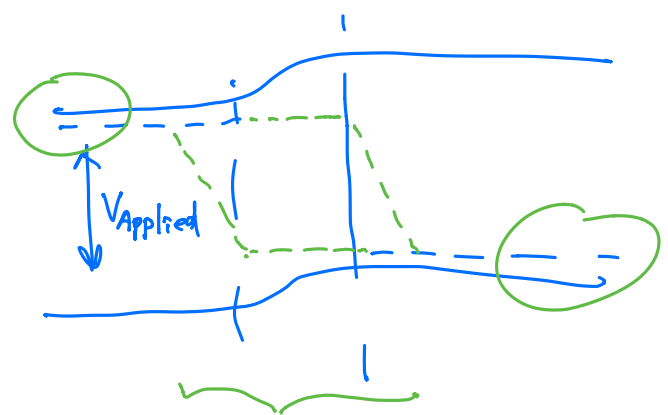
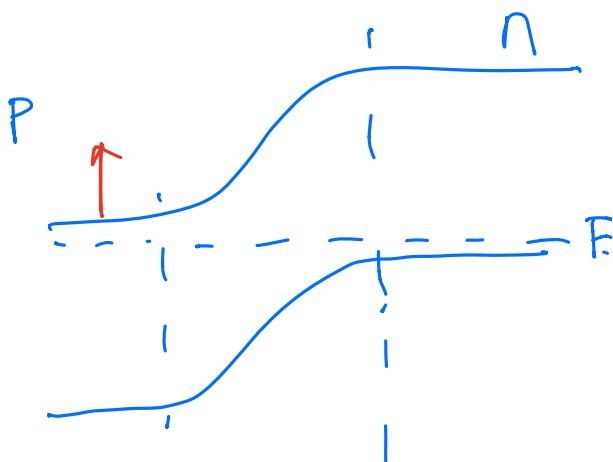
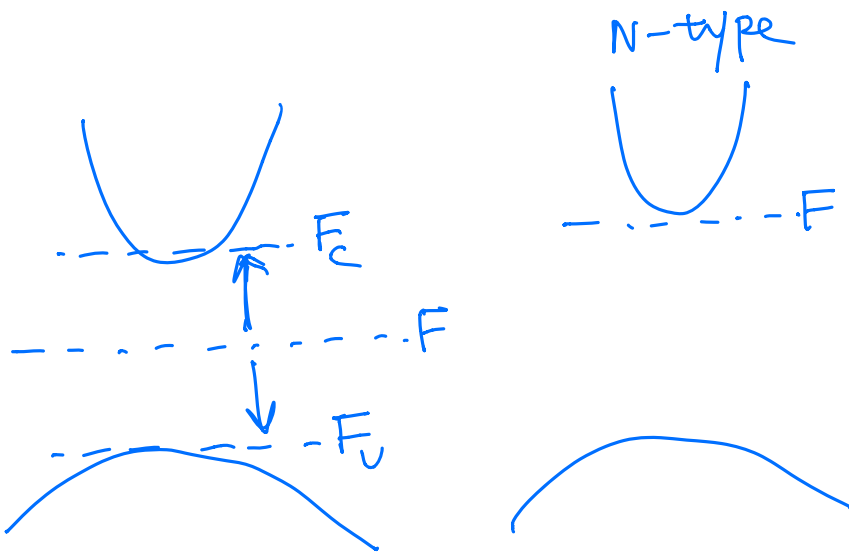
$$E_e = E_c + E_{ni} + \frac{\hbar^2 k^2}{2m_e^*}$$

$$E_k = E_e - (E_c + E_{ni}) = \frac{\hbar^2 k^2}{2m_e^*} \Rightarrow dE_k = \frac{2\hbar^2}{2m_e^*} k dk$$

$$\frac{2}{C} \sum_{\mathbf{k}} = \frac{2}{V} \int \frac{2\pi k dk}{\left(\frac{2\pi}{L_x}\right) \left(\frac{2\pi}{L_y}\right)} = \frac{1}{\pi L_z} \int k dk = \underbrace{\frac{1}{\pi L_z} \frac{m_e^*}{\hbar^2}}_{P_{e,2d}} \int dE$$

Q.W. $n_{2D} = \int P_{e,2d}(E) \cdot f_c(E) dE$

Question about Quasi-Fermi levels



lots of electrons and holes

Question about $\langle u_c | \vec{P} | u_v \rangle$ in bulk semiconductor

$$|\langle u_s | P_x | u_x \rangle|^2 = 3 M_b^2$$

Intuitively, you can think $u_v \sim \frac{1}{\sqrt{3}} u_x + \frac{1}{\sqrt{3}} u_y + \frac{1}{\sqrt{3}} u_z$

$$|\langle u_c | P_x | u_v \rangle|^2 = M_b^2$$

$$\begin{aligned} \hookrightarrow \frac{1}{\sqrt{3}} u_x &\iff \frac{1}{\sqrt{3}} \langle u_c | P_x | u_x \rangle \\ &\frac{1}{\sqrt{3}} u_y \\ &\frac{1}{\sqrt{3}} u_z \end{aligned}$$